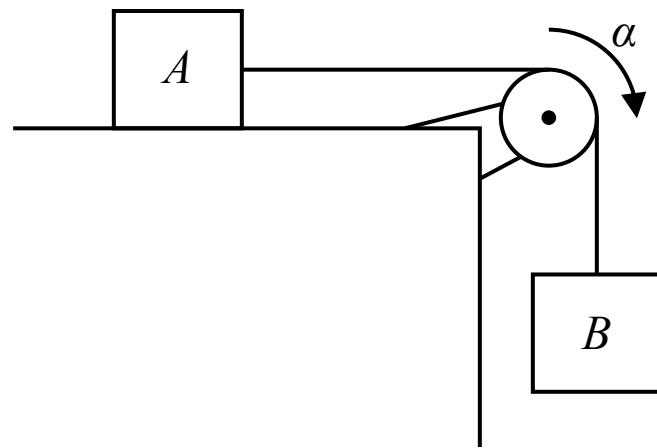
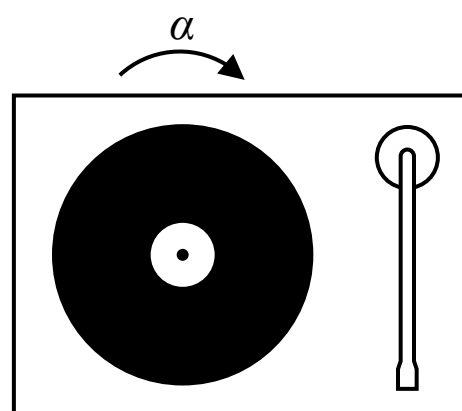
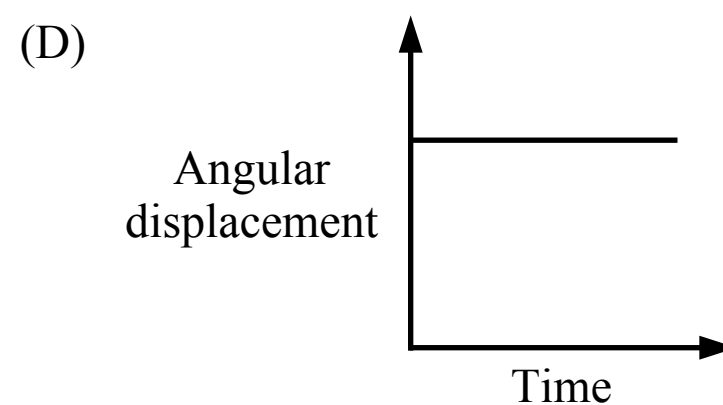
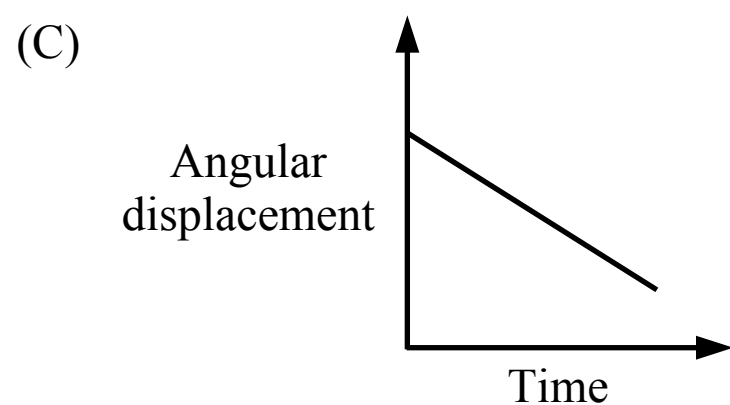
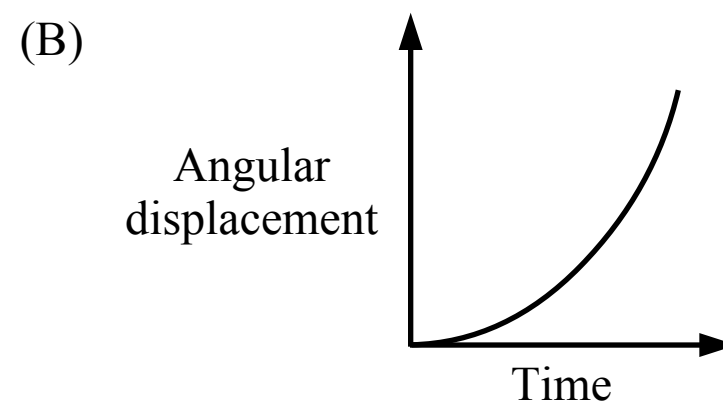
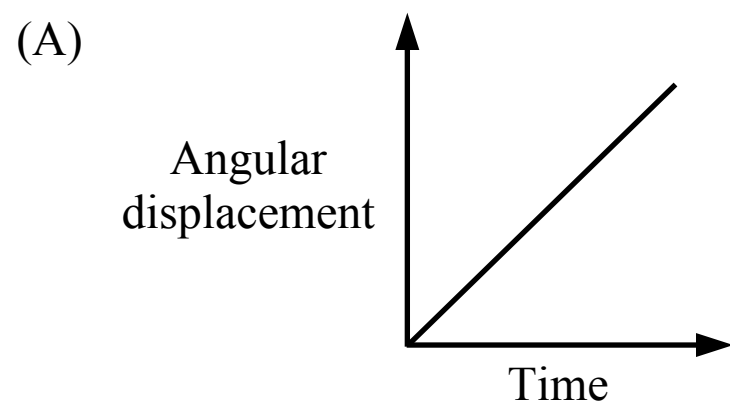


# ROTATIONAL MOTION



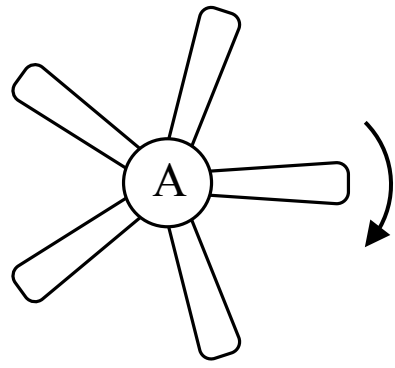
1. Two blocks are connected by a string that passes over a pulley as shown in the figure above. The blocks are released from rest, block B falls and the pulley experiences an angular acceleration. Which of the following graphs could represent the magnitude of the angular displacement of the pulley over time?



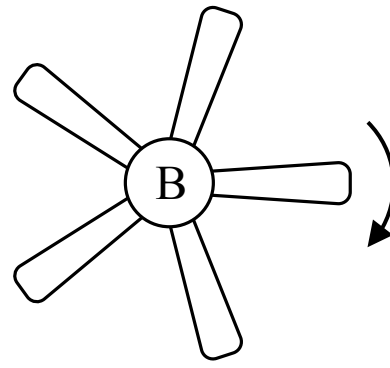
2. A vinyl record begins at rest and then experiences an angular acceleration of  $\alpha$ . What is the angular displacement of the record after a period of 3 seconds?

- (A)  $6\alpha$   
 (B)  $9\alpha$   
 (C)  $3\alpha$   
 (D)  $9\alpha/2$

$$\omega_0 = 1 \text{ rad/s} \quad \alpha = 2 \text{ rad/s}^2$$

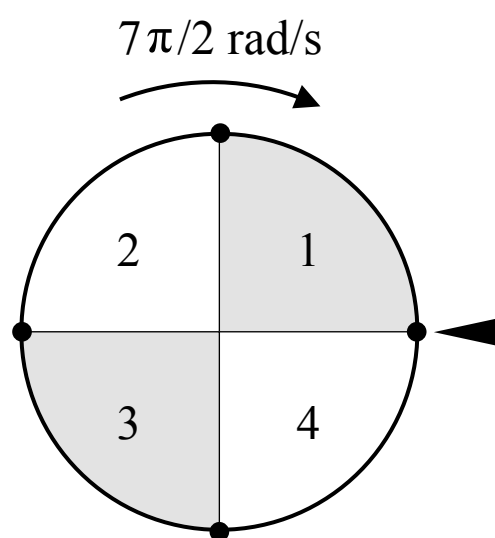


$$\alpha = 3 \text{ rad/s}^2$$



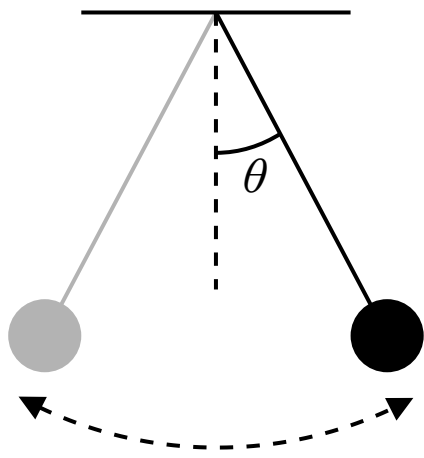
3. Two ceiling fans are shown in the figure above. At time  $t_0$ , fan A is spinning at  $1 \text{ rad/s}$  and begins accelerating at  $2 \text{ rad/s}^2$ , while fan B starts from rest and accelerates at  $3 \text{ rad/s}^2$ . What is the relationship between the angular speed of the fans after a period of 5 seconds?

- (A)  $\omega_A < \omega_B$
- (B)  $\omega_A > \omega_B$
- (C)  $\omega_A = \omega_B$
- (D) Cannot be determined

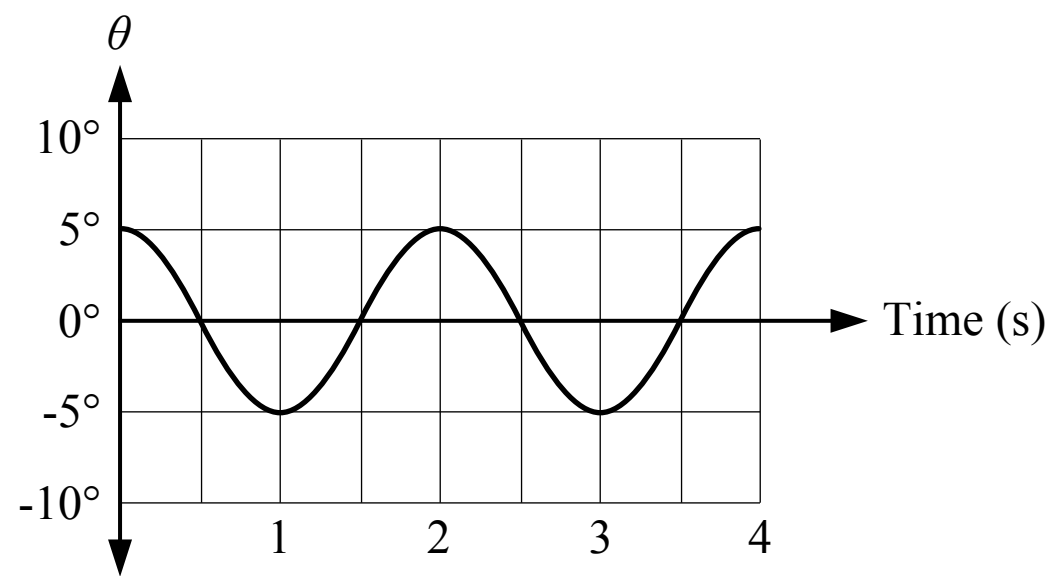


4. A wheel is divided into 4 equal sections as shown in the figure above. The wheel is given a spin and released so that the initial angular speed of the wheel is  $7\pi/2 \text{ rad/s}$  when the wheel is in the orientation shown above. The wheel slows down at a rate of  $-\pi/2 \text{ rad/s}^2$ . What numbered section is the arrow on the right pointing to when the wheel stops?

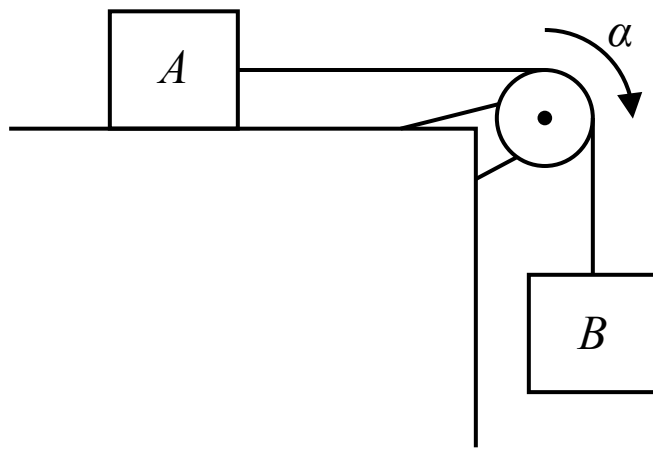
- (A) 1
- (B) 2
- (C) 3
- (D) 4



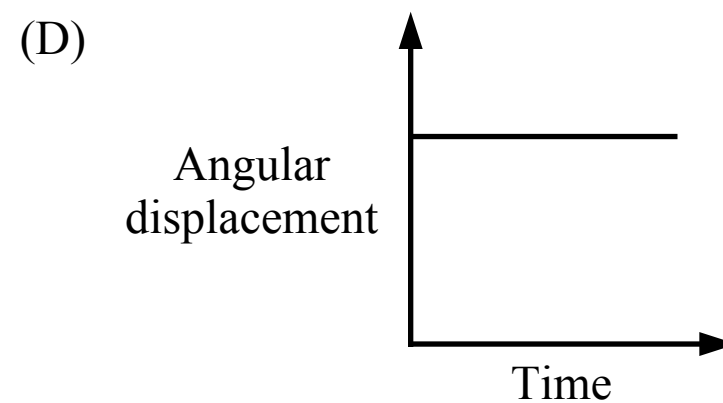
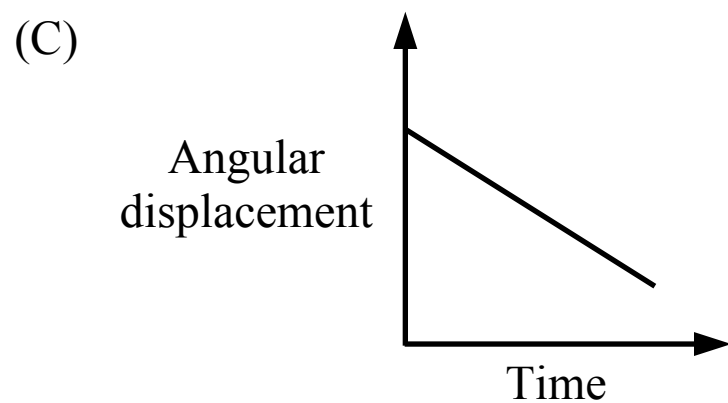
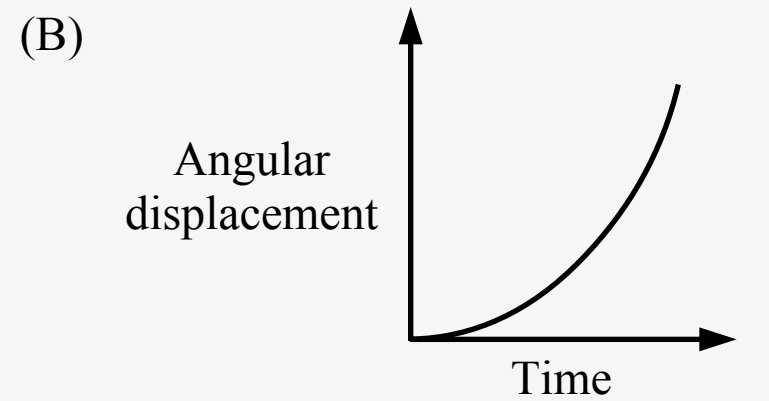
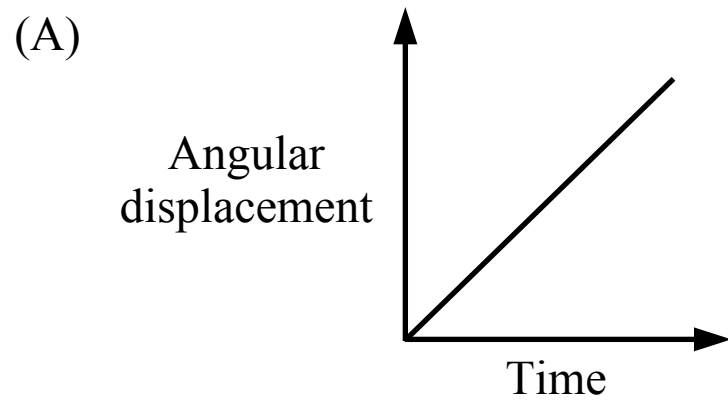
Note: Figure not drawn to scale



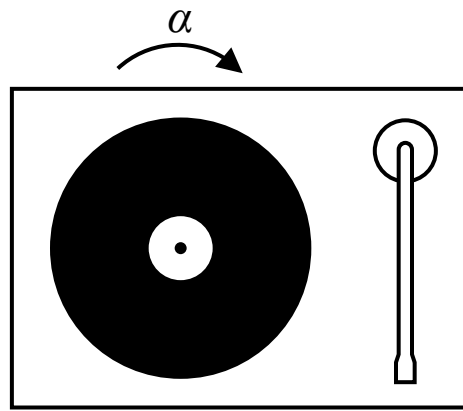
5. A graph of the motion of a pendulum is shown in the figure above. The angle of the pendulum is measured relative to the vertical. Which of the following is true about the motion of the pendulum?
- (A) The angular velocity of the pendulum at 1.5 seconds is zero
  - (B) The angular velocity of the pendulum at 3 seconds is zero
  - (C) The angular velocity of the pendulum is never zero
  - (D) The angular velocity of the pendulum is always zero



1. Two blocks are connected by a string that passes over a pulley as shown in the figure above. The blocks are released from rest, block B falls and the pulley experiences an angular acceleration. Which of the following graphs could represent the magnitude of the angular displacement of the pulley over time?



- A** Incorrect  
This graph is a straight line with a non-zero slope which represents a constant angular velocity with zero acceleration.
- B** **Correct**  
The pulley experiences an angular acceleration so the angular position-time graph and the angular displacement-time graph is a curved line. The slope of the angular displacement-time graph is the angular velocity, which is changing because there is an angular acceleration.
- C** Incorrect  
This graph is a straight line with a non-zero slope which represents a constant angular velocity with zero acceleration.
- D** Incorrect  
This graph is a straight line with zero slope which represents an angular velocity of zero.



2. A vinyl record begins at rest and then experiences an angular acceleration of  $\alpha$ . What is the angular displacement of the record after a period of 3 seconds?

- (A)  $6\alpha$
- (B)  $9\alpha$
- (C)  $3\alpha$
- (D)  $9\alpha/2$

☐ A Incorrect

☐ B Incorrect

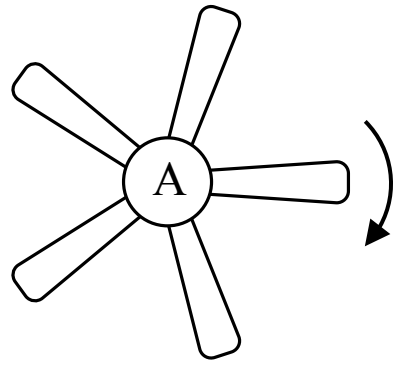
☐ C Incorrect

☒ D **Correct**

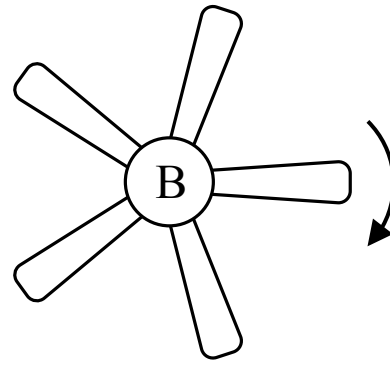
The angular displacement can be found using the kinematic equation below.

$$\Delta\theta = \omega_0 t + \frac{1}{2}\alpha t^2 = (0 \text{ rad/s})(3 \text{ s}) + \frac{1}{2}\alpha(3)^2 = 9\alpha/2$$

$$\omega_0 = 1 \text{ rad/s} \quad \alpha = 2 \text{ rad/s}^2$$



$$\alpha = 3 \text{ rad/s}^2$$



3. Two ceiling fans are shown in the figure above. At time  $t_0$ , fan A is spinning at 1 rad/s and begins accelerating at 2 rad/s<sup>2</sup>, while fan B starts from rest and accelerates at 3 rad/s<sup>2</sup>. What is the relationship between the angular speed of the fans after a period of 5 seconds?

- (A)  $\omega_A < \omega_B$   
 (B)  $\omega_A > \omega_B$   
 (C)  $\omega_A = \omega_B$   
 (D) Cannot be determined

**A Correct**

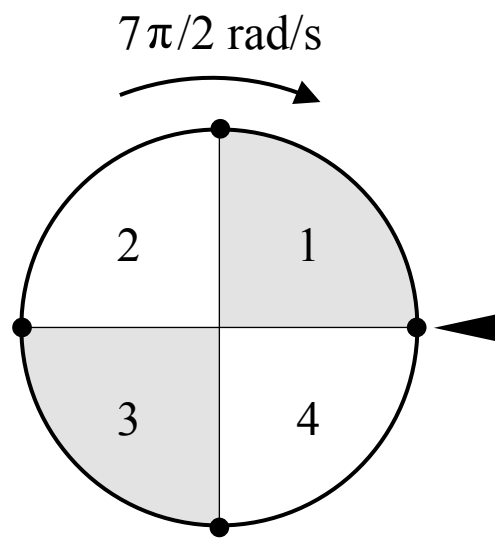
Fan A:  $\omega = \omega_0 + \alpha t = (1 \text{ rad/s}) + (2 \text{ rad/s}^2)(5 \text{ s}) = 11 \text{ rad/s}$

Fan B:  $\omega = \omega_0 + \alpha t = (0 \text{ rad/s}) + (3 \text{ rad/s}^2)(5 \text{ s}) = 15 \text{ rad/s}$

B Incorrect

C Incorrect

D Incorrect



4. A wheel is divided into 4 equal sections as shown in the figure above. The wheel is given a spin and released so that the initial angular speed of the wheel is  $7\pi/2$  rad/s when the wheel is in the orientation shown above. The wheel slows down at a rate of  $-\pi/2$  rad/s<sup>2</sup>. What numbered section is the arrow on the right pointing to when the wheel stops?

- (A) 1  
(B) 2  
(C) 3  
(D) 4

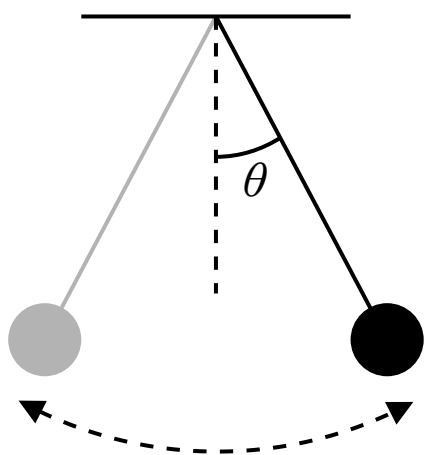
**A Correct**

The angular displacement of the wheel can be found using the kinematic equation below. The wheel turns 6 full revolutions and then 1/8 of a revolution so it ends at the middle of section 1.

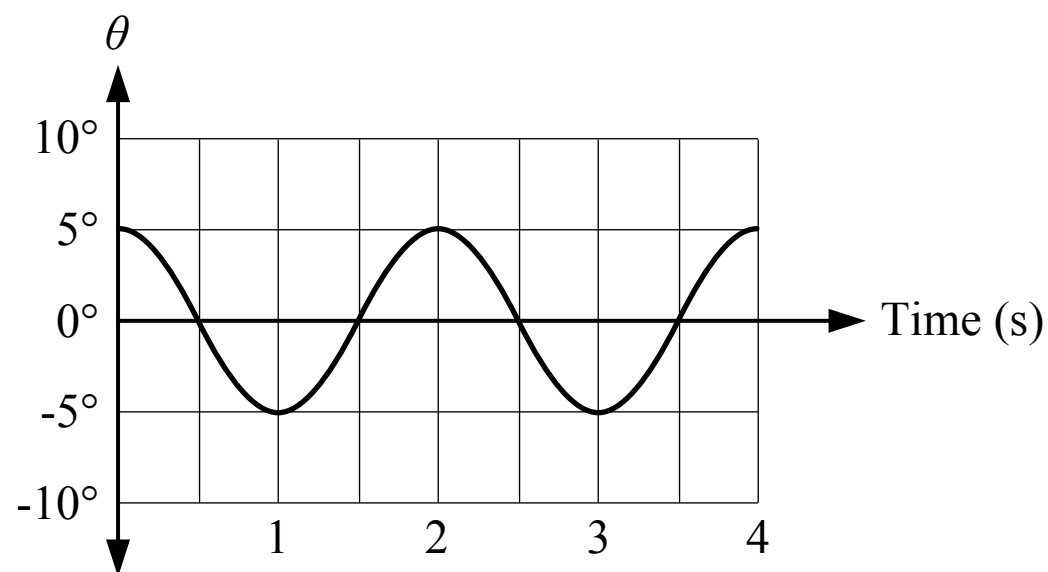
$$\omega^2 = \omega_0^2 + 2\alpha\Delta\theta \quad (0 \text{ rad/s})^2 = (7\pi/2 \text{ rad/s})^2 + 2(-\pi/2 \text{ rad/s}^2)\Delta\theta \quad \Delta\theta = 49\pi/4 \text{ rad}$$

$$\Delta\theta = \frac{49\pi/4 \text{ rad}}{2\pi \text{ rad}} \times \frac{1 \text{ rev}}{2\pi \text{ rad}} = 6 \frac{1}{8} \text{ rev}$$

- (B) Incorrect  
(C) Incorrect  
(D) Incorrect



Note: Figure not drawn to scale



5. A graph of the motion of a pendulum is shown in the figure above. The angle of the pendulum is measured relative to the vertical. Which of the following is true about the motion of the pendulum?

- (A) The angular velocity of the pendulum at 1.5 seconds is zero
- (B) The angular velocity of the pendulum at 3 seconds is zero
- (C) The angular velocity of the pendulum is never zero
- (D) The angular velocity of the pendulum is always zero

**A** Incorrect

The angular position is zero at 1.5 seconds but the angular velocity (the slope) is not zero.

**B** **Correct**

The graph is an angular position-time graph so the slope of the graph is the angular velocity. The slope of the graph and the angular velocity are zero at 3 seconds.

**C** Incorrect

The angular velocity (the slope) is zero at 0, 1, 2, 3 and 4 seconds.

**D** Incorrect

The angular velocity (the slope) is not always zero.